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Measurement of the Michel parameters and the average tau-neutrino helicity from tau decays at LEP

L3 Collaboration

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Abstract

Four of the Michel parameters and the average tau-neutrino helicity have been measured by analysing tau decay spectra in 147 pb^{-1} of data collected by the L3 detector. The decays $\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e$, $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$, $\tau^- \rightarrow \pi^- \nu_\tau$, $\tau^- \rightarrow \rho^- \nu_\tau$ and their charge conjugates were considered. The results: $\rho = 0.762 \pm 0.035$, $\eta = 0.27 \pm 0.14$, $\xi = 0.70 \pm 0.16$, $\xi\delta = 0.70 \pm 0.11$ and $\xi_h = -1.032 \pm 0.031$ are consistent with a V – A structure for the weak charged current and lepton universality. © 1998 Elsevier Science B.V. All rights reserved.

1. Introduction

The Standard Model [1] has proved to be highly successful at explaining the wealth of precise measurements made by the LEP experiments and SLD on the weak neutral current [2]. Similarly, the Standard Model prediction of a V – A Lorentz structure for the weak charged current has been shown to be in excellent agreement with results coming from the precise investigation of muon decay [3]. Nevertheless, a global analysis of the data does leave some room for a non-standard contribution to the charged current [4]. The abundant

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production and decay of tau pairs at LEP gives an opportunity to search for such deviations from the $V - A$ current at higher mass scales than muon decay, as well as to test the Standard Model assumption of lepton universality. The hadronic decay modes of the tau also allow the measurement of the tau-neutrino helicity, imposing a further constraint on the Standard Model. In contrast with experiments at lower energies [5,6], the near perfect anti-correlation of the $\tau^+ \tau^-$ helicities and the non-zero tau polarization near the Z peak facilitate these measurements [7–10].

In this paper, we investigate the Lorentz structure of the weak charged current using $e^+ e^- \rightarrow \tau^+ \tau^-$ events around the Z peak collected by the L3 detector at LEP. The chosen observables are four of the Michel parameters [11] ρ , η , ξ and $\xi\delta$, the average tau-neutrino helicity, expressed as the chirality parameter ξ_h , and the tau polarization \mathcal{P}_τ . The measurement is made using a combined fit to the energy spectra in $\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e$, $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$, $\tau^- \rightarrow \pi^- \nu_\tau$ and $\tau^- \rightarrow \rho^- \nu_\tau$ decays⁹ identified in the 1994-95 data sample. These results are then combined with those of the previous L3 publication [8] to form averages for the full 1991-95 data set.

2. Measurement method

Under the most general four-fermion contact interaction Hamiltonian, the charged lepton decay spectra in $\tau^- \rightarrow l^- \nu_\tau \bar{\nu}_l$ may be written as [12]:

$$\frac{1}{\Gamma} \frac{d\Gamma}{dx_l} = H_0^l(x_l) - \mathcal{P}_\tau H_1^l(x_l) \quad (1)$$

$$= h_0^l(x_l) + \eta h_\eta^l(x_l) + \rho h_\rho^l(x_l) - \mathcal{P}_\tau \left[\xi h_\xi^l(x_l) + \xi\delta h_{\xi\delta}^l(x_l) \right], \quad (2)$$

where $x_l = E_l/E_{\text{beam}}$ ($l = e, \mu$) is the normalized lepton energy and $h^l(x_l)$ are kinematical functions.

Similarly, hadronic spectra in $\tau^- \rightarrow h^- \nu_\tau$ are described by

$$\frac{1}{\Gamma} \frac{d\Gamma}{dx_h} = H_0^h(x_h) - \mathcal{P}_\tau H_1^h(x_h) \quad (3)$$

$$= h_0^h(x_h) - \mathcal{P}_\tau \xi_h h_1^h(x_h). \quad (4)$$

For $\tau^- \rightarrow \pi^- \nu_\tau$, $x_\pi = E_\pi/E_{\text{beam}}$. In the case of $\tau^- \rightarrow \rho^- \nu_\tau$, $x_\rho = \omega_\rho$ where ω_ρ is a function of the energies and opening angles of the decay products in $\rho^- \rightarrow \pi^- \pi^0$ which optimizes sensitivity to the tau polarization [13]. Qualitatively, negative values of ω_ρ are enriched by left-handed τ^- , positive values by right-handed τ^- .

The joint decay distribution for $e^+ e^- \rightarrow \tau^+ \tau^- \rightarrow A^\pm B^\mp n \nu$ ($n = 2, 3, 4$) where A, B are e, μ, π or ρ is

$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dx_A dx_B} = H_0^A(x_A) H_0^B(x_B) + H_1^A(x_A) H_1^B(x_B) - \mathcal{P}_\tau \left[H_1^A(x_A) H_0^B(x_B) + H_0^A(x_A) H_1^B(x_B) \right]. \quad (5)$$

By fitting this form to the correlated tau decay spectra from $e^+ e^- \rightarrow \tau^+ \tau^-$, we extract the Michel parameters, the chirality parameter and the average tau polarization up to a sign ambiguity which is solved by reference to other experiments [10,14]. The analysis method follows closely that used in the previous L3 publication [8].

⁹ Formulae are given for τ^- . Charge conjugate decays are implied throughout this paper. Charged pions and kaons are not distinguished.

3. Data sample and event selection

The data analysed in this paper were recorded by the L3 detector [15] at center-of-mass energies around the Z peak in 1994-95, and correspond to an integrated luminosity of 78 pb^{-1} . A sample of Z decays to charged lepton pairs is obtained by applying a pre-selection based on event topology and particle multiplicity. Selected events are then divided into two hemispheres by a plane perpendicular to the thrust axis and particle identification is applied to each hemisphere separately.

For efficiency and background estimates, the following Monte Carlo programs are used: KORALZ [16] for $e^+e^- \rightarrow \tau^+\tau^-(\gamma)$ and $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$, BHAGENE [17] for $e^+e^- \rightarrow e^+e^-(\gamma)$ and DIAG36 [18] for $e^+e^- \rightarrow e^+e^-\bar{f}f$ where $\bar{f}f$ are e^+e^- , $\mu^+\mu^-$, $\tau^+\tau^-$ or $q\bar{q}$. Generated events are passed through a full detector simulation based on the GEANT [19] program. The number of Monte Carlo events for each process is about eight times larger than the data sample.

3.1. Particle identification

Particle identification is restricted to the barrel region of the detector ($|\cos\theta| < 0.7$). Electrons are identified as a track reconstructed in the central tracker that is matched to a narrow shower in the electromagnetic calorimeter. There must be little or no energy in the hadron calorimeter and no associated track in the muon spectrometer. Muons have a track in the muon spectrometer, reconstructed from three precision chamber segments, that extrapolates back to the interaction point with a minimum ionizing response in the calorimeters. There must be an associated track in the inner tracker.

Hadrons are identified using the central tracker and the calorimeters. Tracking information is used to identify the impact point of a charged particle at the electromagnetic calorimeter. An algorithm [20] is applied to disentangle overlapping neutral calorimetric clusters in the vicinity of the impact point and a hadronic shower, whose shape is nearly energy independent, is subtracted from the energy deposit. Electromagnetic neutral identification criteria are applied to the remaining local maxima.

Shower shape and energy cuts are applied to neutral clusters to identify neutral pions via their decay into two photons. For pion energies below 10 GeV, a large fraction of the photons are spatially resolved. Above this energy the showers from the two photons overlap to form a single neutral electromagnetic cluster.

The decays $\tau^- \rightarrow \pi^- \nu_\tau$ are identified as hemispheres that are inconsistent with an electron or muon, containing one charged track, no π^0 candidates and calorimetric energy well matched with the track momentum. The decays $\tau^- \rightarrow \rho^- \nu_\tau$ are identified as hemispheres with one charged track and one π^0 candidate, a total calorimetric energy greater than 5 GeV and an invariant mass of the charged-neutral pair within the range 0.45–1.20 GeV.

3.2. Event selection

Events with at least one identified tau decay are retained and subjected to loose cuts that correlate the information in both hemispheres in order to reduce contamination from non-tau events while introducing minimal distortion of the measured decay spectra. Bhabha, dimuon and two-photon backgrounds are reduced to the level of a few percent by applying cuts on the total visible energy and jet acollinearity and aplanarity. Cosmic muons are rejected by cuts on scintillator timing and the distance of closest approach (DCA) of tracks to the interaction point.

Surviving events are classified according to the tau decay candidate in each hemisphere: ee , $e\mu$, $e\pi$, $e\rho$, eX , $\mu\mu$, $\mu\pi$, $\mu\rho$, μX , $\pi\pi$, $\pi\rho$, πX , $\rho\rho$ and ρX where X represents a hemisphere with no identified tau decay. Backgrounds in each channel coming from misidentified tau decays are estimated from simulated $Z \rightarrow \tau^+\tau^-$ events. Bhabha, dimuon and two-photon background shapes are taken from Monte Carlo and normalized

Table 1

Fit ranges for each channel, numbers of events selected, selection efficiencies ϵ and τ and non- τ background fractions. Only events within the fit range are included in this table.

Channel	Fit range	Events	$\epsilon(\%)$ in 4π	Bkg(%)	
				τ	non- τ
ee	$x_e[0.25,0.75]$	558	19.4	4.2	7.0
e μ	$x_e[0.05,0.95]$	1574	33.7	3.1	0.1
e π	$x_\mu[0.05,0.95]$	1489	36.3	12.3	2.3
	$x_\pi[0.05,0.95]$				
e ρ	$x_\pi[0,1.4]$	2817	34.1	14.9	0.4
	$x_e[0.05,0.95]$				
eX	$\omega_\rho[-1,1]$	6176	66.5	2.5	4.3
	$x_e[0.05,0.95]$				
$\mu\mu$	$x_\mu[0.05,0.75]$	437	22.0	0.6	1.0
$\mu\pi$	$x_\mu[0.05,0.95]$	1002	27.6	11.5	0.6
	$x_\pi[0,1.4]$				
$\mu\rho$	$x_\mu[0.05,0.95]$	1892	26.9	13.2	0.3
	$\omega_\rho[-1,1]$				
μX	$x_\mu[0.05,0.95]$	3897	49.1	0.7	1.0
$\pi\pi$	$x_\pi[0,1.4]$	456	30.8	20.6	2.1
$\pi\rho$	$x_\pi[0,1.4]$	1921	30.2	22.3	0.8
	$\omega_\rho[-1,1]$				
πX	$x_\pi[0,1.4]$	4088	58.4	12.0	1.1
$\rho\rho$	$\omega_\rho[-1,1]$	1816	28.8	23.4	0.1
ρX	$\omega_\rho[-1,1]$	7500	55.5	12.8	0.3
Total		35623			

using the number of such events estimated to be present in the selected data sample. Background from cosmic muons is estimated using a control sample of data selected by loosening the cut on the track DCA.

The measured spectra are fitted over the full acceptance range except in the case of electrons and muons, where the fit is restricted to regions where the background is small. The fit range for each channel, number of selected events, selection efficiency and the tau and non-tau background fractions are shown in Table 1.

4. Fit procedure

We perform a simultaneous measurement of ρ , η , ξ , $\xi\delta$, ξ_h and \mathcal{P}_τ using a binned maximum-likelihood fit to the decay spectra of selected events. In the case where only one hemisphere has an identified tau decay, the one-dimensional spectrum of the identified particle is used. If both hemispheres are identified the decay variables of both particles are used to form a two-dimensional correlated decay spectrum.

The fit procedure is described in detail in Ref. [8]. The likelihood function is

$$\mathcal{L} = \prod_{i,j} \frac{(w_{ij}(\alpha) + b_{ij})^{n_{ij}} e^{-(w_{ij}(\alpha) + b_{ij})}}{n_{ij}!}, \quad (6)$$

where n_{ij} is the number of data events observed in the j -th bin of the i -th decay mode, $w_{ij}(\alpha)$ is the expected number of signal events for a particular set of parameters $\alpha = \{\rho, \eta, \xi, \xi\delta, \xi_h, \mathcal{P}_\tau\}$ and b_{ij} is the sum of tau and non-tau background. The dependence of the tau-background on α is taken into account.

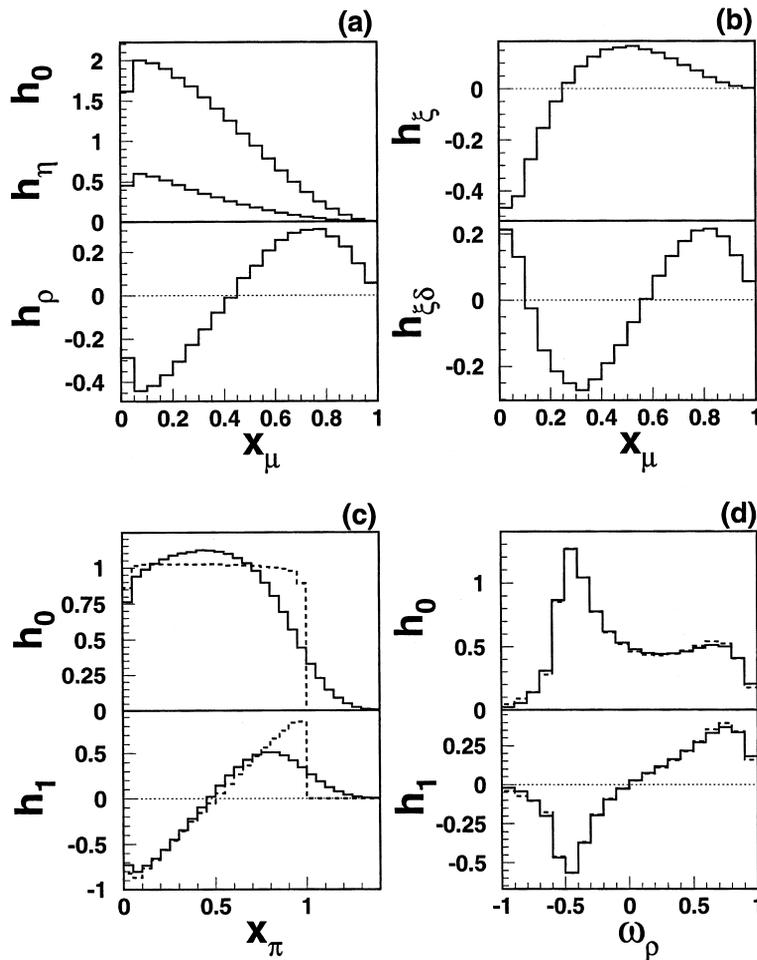


Fig. 1. Kinematical functions used to fit (a)(b): μ spectra from $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$, (c): π spectra from $\tau^- \rightarrow \pi^- \nu_\tau$ and (d): ρ spectra from $\tau^- \rightarrow \rho^- \nu_\tau$. The functions used to fit electron spectra from $\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e$ are very similar to (a) and (b) apart from h_η^e which is suppressed by a factor of $(m_e/m_\mu)^2$ relative to h_η^μ . In (c) and (d), the dashed histograms correspond to generator level Monte Carlo; the solid histograms include detector resolution and acceptance. For (a) and (b), the effect of resolution and acceptance on the curves is not visible on this scale.

Each $w_{ij}(\alpha)$ is given by a convolution of the appropriate kinematical functions with the detector resolution and acceptance. The total number of expected signal and background events is fixed to the total number of events selected in the data for each decay channel.

Table 2
Correlation coefficients for the fit to 1994–95 data.

	η	ξ	$\xi\delta$	ξ_h	\mathcal{P}_τ
ρ	0.54	-0.20	-0.27	-0.14	0.22
η		0.13	0.04	0.01	0.03
ξ			0.12	0.11	0.06
$\xi\delta$				0.16	-0.15
ξ_h					-0.30

The kinematical functions are obtained using linear combinations of decay spectra generated by KORALZ with a modified version of the TAUOLA [21] τ decay library that allows the generation of samples with any combination of Michel parameters. Functions for μ , π and ρ are shown in Fig. 1. Fig. 1 also shows the effect of the convolution of the kinematical functions for $\tau^- \rightarrow \pi^- \nu_\tau$ and $\tau^- \rightarrow \rho^- \nu_\tau$ with the detector resolution and acceptance.

5. Results

The results of the fit to the leptonic and hadronic decay channels in the 1994-95 data are:

$\rho = 0.724$	± 0.043	± 0.021	(0.75)
$\eta = 0.26$	± 0.19	± 0.08	(0)
$\xi = 0.51$	± 0.19	± 0.09	(1)
$\xi\delta = 0.62$	± 0.14	± 0.06	(0.75)
$\xi_h = -1.065$	± 0.033	± 0.016	(-1)
$\mathcal{P}_\tau = -0.173$	± 0.016	± 0.014	

where the first error is statistical and the second systematic. For comparison, the Standard Model predictions are shown in parentheses. The correlation coefficients between the parameters are shown in Table 2. Estimation of the systematic errors is described below. Examples of the fit result in comparison to the data are shown in Figs. 2 and 3.

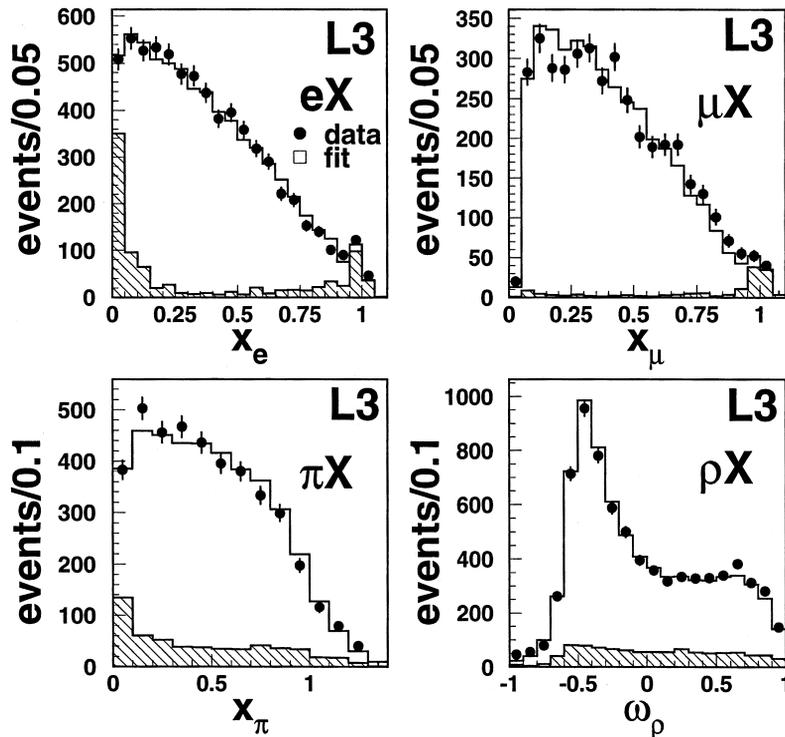


Fig. 2. 1994-95 data and fit result for the eX , μX , πX and ρX final states, where X represents an unidentified τ decay. The shaded histograms show the sum of τ and non- τ background.

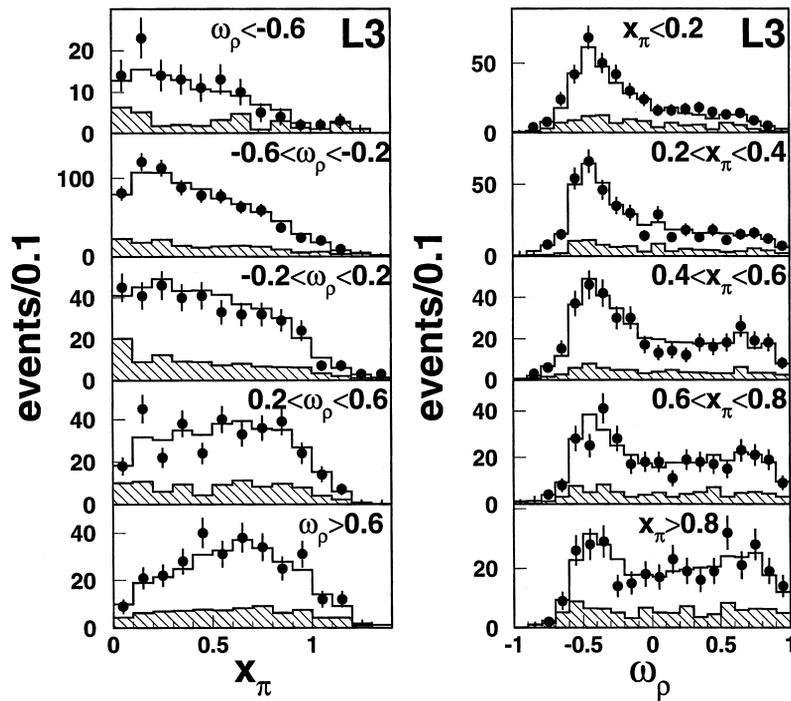


Fig. 3. 1994-95 data (points) and fit result (histogram) in the $\pi\rho$ channel. On the left are pion energy spectra for different slices of the ω_ρ variable. On the right are distributions of ω_ρ for different slices in pion energy. The shaded histograms show the sum of τ and non- τ background.

In a separate analysis that considers only the hadronic decay channels but includes a re-analysis of the 1991-93 data, the chirality parameter ξ_h and the tau polarization \mathcal{P}_τ have been independently determined [22]. Good agreement between the two analyses is seen.

6. Systematic errors

We considered the following sources of systematic error: event selection, background estimation, the energy calibration of the detector, and the use of finite Monte Carlo statistics. These sources are considered to be independent.

To determine the systematic error due to event selection, we varied the correlated cuts between hemispheres by amounts corresponding to the estimated inaccuracy of the Monte Carlo simulation for each cut variable. The error due to the uncertainty in the background coming from mis-identified tau-decays was estimated by varying the largest decay branching fractions of the tau by their experimental errors [4]. Non-tau background systematics were estimated by varying the normalization of all non-tau backgrounds by their statistical errors.

The error due to detector calibration uncertainties was estimated by varying the appropriate energy scales by their known uncertainty. The momentum scale of the central tracker is known to 0.5% from a comparison of its muon momentum measurements and those of the muon spectrometer. The accuracy of the energy scale of the electromagnetic calorimeter is known from the position of the π^0 peak to be 0.5% below 5 GeV, and from Bhabha events to be 0.05% at 45 GeV. The energy scale of the hadron calorimeter is accurate to 1%, as estimated from the peak position of the ρ resonance. The momentum scale of the muon spectrometer is known

Table 3
Summary of systematic errors for 1994-95 data.

Uncertainty	$\Delta\rho$	$\Delta\eta$	$\Delta\xi$	$\Delta\xi\delta$	$\Delta\xi_h$	$\Delta\mathcal{P}_\tau$
Selection	0.003	0.01	0.04	0.01	0.005	0.003
Background	0.010	0.03	0.02	0.02	0.006	0.003
Calibration	0.010	0.02	0.04	0.03	0.007	0.012
MC statistics	0.015	0.07	0.07	0.05	0.012	0.006
Total	0.021	0.08	0.09	0.06	0.016	0.014

from dimuon events to be accurate to 0.05%. Below 5 GeV the muon momentum measurement is dominated by energy loss in the calorimeters and the scale is known to 0.5%. At low energy, a cross-check of the calibration of the central tracker with the electromagnetic calorimeter and the muon spectrometer is performed using electrons and muons from tau decays and two-photon events.

The contribution of each systematic error is given in Table 3.

7. Combination of results

The results obtained from the fit to the 1994-95 data are combined with those of the previous L3 publication [8] to obtain averages for the 1991-95 data set, corresponding to a total integrated luminosity of 147 pb^{-1} :

$$\begin{aligned}
 \rho &= 0.762 && \pm 0.035 \\
 \eta &= 0.27 && \pm 0.14 \\
 \xi &= 0.70 && \pm 0.16 \\
 \xi\delta &= 0.70 && \pm 0.11 \\
 \xi_h &= -1.032 && \pm 0.031 \\
 \mathcal{P}_\tau &= -0.164 && \pm 0.016
 \end{aligned}$$

The combined correlation coefficients are given in Table 4. In making this average, the systematics due to event selection were considered to be completely correlated between the two sets of measurements. The remaining systematic errors were treated as independent.

The values obtained for the Michel parameters are in agreement with a V – A structure of the weak charged current in decays of the tau lepton and support the Standard Model assumption of lepton universality. The measured chirality parameter ξ_h is in agreement with the assumption of only left-handed neutrinos in semileptonic tau decays. The mean tau polarization is consistent with the results from a separate analysis of the

Table 4
Correlation coefficients for the combined 1991-95 results.

	η	ξ	$\xi\delta$	ξ_h	\mathcal{P}_τ
ρ	0.50	-0.19	-0.26	-0.21	0.32
η		0.13	0.06	0.00	0.03
ξ			0.07	0.11	0.11
$\xi\delta$				0.25	-0.19
ξ_h					-0.35

L3 data [23] that focuses on the measurement of neutral couplings and assumes a $V - A$ structure for the tau decay vertex.

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